



where  $n_{m\uparrow}$  and  $n_{m\downarrow}$  denote the occupation of the  $m$  sublevel of spin  $\uparrow$ , and the occupation of the host material without doping. The parameter  $\mu$  can be tuned to fulfil the linearity of  $E(N)$ , i.e., the generalized Koopmans condition:

$$n_k = E(N-1) - E(N) + \epsilon_{\text{ig}}(N) = 0, \quad (2)$$

where  $E(N-1) - E(N)$  denotes the total energy cost to rem