LCAO TRUNCATED CRYSTAL CALCULATIONS ON SOME ELECTRONIC PROPERTIES OF

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1. INTRODUCTION

The truncated crystal approach to the description of electronic properties of covalent solids, has been successfully applied in recent years to a large variety of

hydrogen in the laboratory[12, 14], and because of interest in laser production of hydrogen plasma from cold solid hydrogen, for use in thermonuclear reactions[15]. The former problem, treated from the point of view of

[CAO representation or hy Slater's Va method[7] and

one electron energy states in the malegular phase with

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properties, namely: to what extent it is possible to lower

theory[10] and defect molecule[11] approaches to the

suggested to lower the energy of the first electronic

atom or molecule with different electronegativity than the host crystal, has been substituted[5].

These advantages of the truncated crystal approach are used in this paper to calculate various electronic properties of molecular hydrogen crystals.

Much theoretical effort has been devoted lately to the investigation of properties of compressed solid hydrogen at low temperatures, mainly due to the interesting possibility of producing a high pressure phase of metallic

states and their separation from the bottom of the conduction band.

In Section 2 we describe the molecular cluster method and specify the quantum mechanical methods that are used with it. In Section 3 we treat some one-electron states in the crystal (corresponding to energies of ionization and edge of conduction band) and in Section 4 the Frenkel exciton states are discussed by the same method. In Section 5 we present some model calculations on impurity states in solid hydrogen.

2. DESCRIPTION OF THE MOLECULAR CLUSTER MODEL

The electronic wave functions of a crystal in the LCAO

taken as -13.6 eV and Δ_{μ} as -14.0 eV [22]. S_{μ} are calculated using Slater orbitals with the best variational exponent of 1.2. After obtaining an initial guess for the

$$\phi_i = \sum_{\nu=1} C_{\nu i} \chi_{\nu} \qquad i = 1, 2 \dots N \tag{1}$$

where χ_{ν} denote the atomic orbitals on site ν . The C_{ν} are the solutions to the one-electron Hartree-Fock equations

formed by taking a central molecule and adding successive shells of neighbours (13, 18, 43, 55, 77 molecules for 1, 2, 3, 4, 5 orders of neighbours, respectively). Since we are not interested in the properties of the small clusters



The ϵ_i are the one-electron crystal orbital energies, $F_{\mu\nu}$ are the matrix elements of the one-electron effective Hamiltonian in the frame of the atomic orbitals and $S_{\mu\nu}$ are overlap integrals between these atomic orbitals. We are interested in the solutions of (2) both for the case of a defect placed in the crystal, and for the crystal maintaining perfect translational symmetry. We would also be interested in correlating the properties of the crystal orbitals belonging to the localized defect state with states of the ideal crystal. Therefore, instead of factorizing the secular problem (2) by considering translational symmetry, we propose to solve (2) directly under some simplifying assumptions on $F_{\mu\nu}$, as a function of N, for

the bulk values with no relaxations allowed. The coefficients C are then used to calculate the set atomic charges Q_μ for an the atomic and the eyest repeated until convergence of 0.005 e is obtained between successive iterations. The atomic charges are computed from one and two center contributions to the charge moments by a procedure that leaves the projection of the centroid of charge, onto the line connecting the two atoms, unchanged [22]. This avoids the usual procedure of dividing the bond charge equally between the atoms involved, a procedure that yields erroneous results when the atoms involved have different electronegativities.

The one-electron energy levels obtained, are populated

with N electrons and the band gap is defined as the

difference between highest occupied and lowest vacant cluster states, while the Koopman's cluster ionization potential is taken as the negative of the energy of the highest accurated state. The desiration of the Mulliban

closely related to the Cusacks approximation employed here from Hostree Fook constitute [24, 25], shows that for systems with relatively homogeneous emarge distribution,

the one perturbed by a point defect, as N as increased.

The converges of such property is exemined for various defisites, through a charge sen-consistent solu-

previously applied to lattice dynamic properties of atomic solids [18, 19] and to electronic properties of atomic [1-6] and molecular [20] solids.

The matrix elements $F_{\mu\nu}$ are approximated either by the

equilibrium internuclear separation, this procedure yields a ionization potential of 15.38 eV compared with the experimental [26] value of 15.43 eV, an $X^{1}\Sigma_{1k}$ to $B^{1}\Sigma_{1k}$ one-electron energy gap of 10.965 eV as compared with

diagonal matrix element are given by:

$$F_{\mu\nu} = S_{\mu\nu} [H_{\mu\mu}(Q_{\mu}) + H_{\nu\nu}(Q_{\nu})] \times (1 - 0.5|S_{\mu\nu}|)$$
 (3)

value of 4.66 eV as compared with the experixntal value of 4.474 eV [26].

In the INDO approach, the off diagonal matrix element is taken as

 $F_{\mu\nu} = \beta^{\circ}_{AB} S_{\mu\nu} - \frac{1}{2} P_{\mu\nu} \gamma_{AB}$

(5)

dependent through the relation

$$H(O) = H^{\circ} + O \Lambda$$

and the diagonal elements are

and $H^{\circ}_{\mu\mu}$ is the Hartree-Fock free atom one-electron orbital energy for the μ th orbital, and Δ_{μ} is the change in orbital energy per unit charge. A minimal basis set of Slater orbitals is employed. For hydrogen 1s state, $H^{\circ}_{\mu\mu}$ is

$$F_{\mu\mu} = U_{\mu\mu} + (P_{AA} - \frac{1}{2}P_{\mu\mu})\gamma_{AA} + \sum_{B \neq A} (P_{BB}\gamma_{AB} - V_{AB})$$
(6)

where the bonding parameter β_{AB}° is determined empiri-

cally to give an overall best fit to accurate LCAO-SCF

15.4

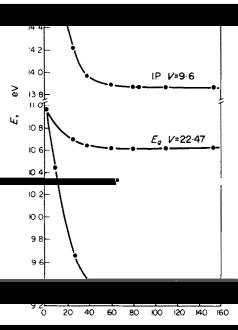
Roothaan [27]. When the electron repulsion integrals are not parametrized, the agreement for H₂ properties with experiment is quite poor [23]. We followed the original formulation (equations 5-6) of Pople et al. [23], and used the INDO approach in truncated crystal calculation only to a limited extent, due to its failure to account reasonably for the free molecule properties (although different parametrization schemes could produce a better agreement).

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IN SOLID Pa3 HYDROGEN

Figure 1 represents the calculated band gap and ionization potential for Pa3 clusters of increasing number of molecules as obtained in the truncated crystal calculations with IEXH calculations. For 3 orders of neighbours, convergence is obtained even for the highest density

occupied crystal orbital energies) and ionization potential



Eig. 1. Variation of ignitation naturals (ID) and hand con (E.)

form plusters and further decrease is obtained as the

value is providing not adequately described by the infilling

valence band, no attempt was made to further increase the density of the cluster towards the metal hydrogen limit.

The convergence of the band gap and ionization potential as a function of cluster size, as obtained by applying the INDO approximation to the matrix elements as already noted, yields poor agreement even with isolated molecule experimental data for these properties, the values obtained for cluster calculation are not of much interest, and we will proceed with the IEXH approximations to

nitride [5a] and diamond [2, 4] where the bonded atomic interactions tend to accumulate excess charge on the unsaturated atoms at the surface), no attempt has been made to apply periodic boundary conditions to suppress charge inhomogeneity. This however would probably be important in similar bracks on atomic hydrogenerystals [28].

In Fig. 3, the density dependence of some calculated electronic properties of solid Pa3 hydrogen is revealed, as obtained in the cluster calculation with IEXH approxima-

mentioning that the relative decrease in ionization potential and band gap, as a function of cluster size, is similar in both methods, indicating that cluster models of this size are probably sufficient to describe these properties in the bulk.

Since the charge distribution over the atoms in the molecular cluster was relatively homogeneous even at the clusters surface (contrary to the situation in clusters

corresponding to the free molecule values, coincide with the values obtained by the same method of calculation for a single molecule. For the experimental equilibrium volume ($V = 22.47 \text{ cm}^3/\text{mole}$, a = 5.2875 Å) the band gap in the cluster is 10.7 eV, as compared with the lower edge of the singlet-singlet absorption of solid D_2 obtained by Baldini [29] in the u.v. spectrum, of 10.8 eV. For the highest density considered ($V = 9.6 \text{ cm}^3/\text{mole}$), the gap

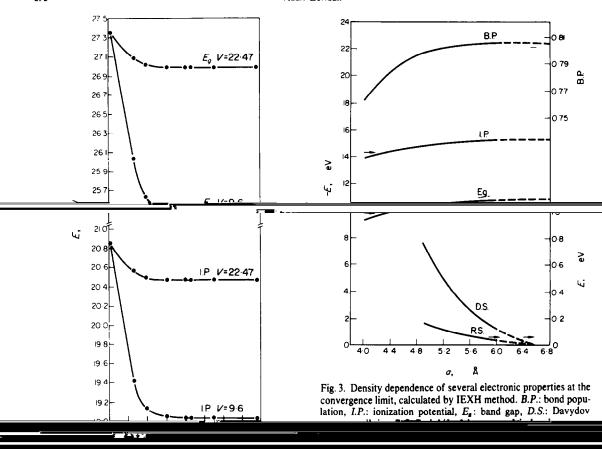


Fig. 2. Variation of ionization potential (I.P.) and band gap (E_t) with cluster size for two volumes (V in cm³/mole) as calculated for INDO clusters.

decreases to 9.2 eV*. It is also observed that the decrease in the band gap is mainly due to the decrease of the energy

that are lower than those obtained by the molecular cluster approximation, reaching at the limit of very low density to an overestimation of 5 GeV of the experimental ionization potential. This large deviation both from experimental results at very low densities and from the

equilibrium volume and rises to 4.94 eV at $V = 9.6 \text{ cm}^3/\text{mole}$.

An citarap: 4s calculate electronic energy changes in solid molecular hydrogen due to density changes, was

metallic forms [13, 14].

The binding energy per molecule, is calculated in the charter model by summing the one electron energy levels of all occupied states. Since LCAO treatment of closed

function outside the molecular Wigner-Seitz sphere. Extending this calculation to lower densities, shows that the Wigner-Seitz model results in one-electron energies

*This decrease in excitation energy upon compression is probably too low for increasing significantly the absorption

of our cluster calculation with the phenomenological form of pair interaction

$$\phi_{rep} = 4\epsilon \left(\frac{\sigma}{r}\right)^{12} \tag{7}$$

we get for 3.70 Å < r < 3.80 Å, taking the accepted value

(10)

as compared with the experimental value of the bulk crystal of 36.7°K deduced from compressibility and second virial coefficient data[32]. Reasonable agreement

where

$$L_{ni,01}^{s} = \sum_{n} \langle \phi_{ni}^{s} \phi_{01}^{o} | V_{ni,01} | \phi_{ni}^{o} \phi_{01}^{s} \rangle = \sum_{n} I_{ni}^{s}$$
 (9)

cluster approximation, was previously obtained also for N_2 - N_2 interaction [20].

A different representation of the interaction in the crystal could be obtained by calculating the change in bond normalization[22] of the central molecule in the cluster.

the strength of the molecular bond at various crystal densities. It is evident that upon compression of the unit cell, keeping the molecular bond length constant, this bond is weakened due to extraction of electronic charge

from the region between two bonded hydrogen atoms.

 $\Delta \epsilon^s$ is the free molecule excitation energy to state s and $V_{ni,mi}$ is the intermolecular potential (in equation 10 the

 $\lambda=1$ is of A_u symmetry while the states $\lambda=2,3,4$ belong to the triply degenerate T_u representation. Since for dipole allowed states in the Pa3 structure, all $L_{n,01}$ are equal, we denote $J'=L_{n,01}$ for $\lambda=2,3,4$ and $J=L_{n,1,01}$, adopting the notation of Hexter for vibrational excitons [36]. The splitting between the T and A states

We next consider the energies of the Frenkel exciton states in molecular solid hydrogen by the same LCAO approach.

 $(D^s+J).$

The pression of the excitor states will be evaluated in

direct solution of the LCAO problem for H_2 dimers oriented mutually as pairs in the crystal; (b) expansion of the $L_{\pi,001}$ matrix elements in multipole series and retention

factor group. A group theoretical analysis reveals that the free molecule (point group $D_{\pi h}$) ground state ${}^{1}\Sigma_{1g}$ yields in the $T_{\pi h}$ factor group a totally symmetric representation

excited state.

(a) The splitting between the excited states of a H_2 dimer formed from molecules 1 and 2, is twice the

while the transition to the triply degenerate T_u state is dipole allowed and polarized along the x, y, z unit cell directions. The transition to the free molecule zero vibrational state of $B^{1}\Sigma_{1u}$ occurs at 11·235 eV [26] and at 11·181 eV in D and H respectively. The greatest energy of solid D_2 at 6°K [29] reveals an absorption edge at 10·8 eV originating from the same molecular transition, followed by a relatively broad absorption band peaking at about 12 eV. At higher energies this absorption overlaps with the lower part of the $2p^{1}\Pi_{u}$ absorption. The energy

ranging to 6 orders of neighbours. The dimers oneelectron energies are computed by IEXH method (equation 3) with the atomic parameters mentioned in Section 2. This yields at normal density, a splitting of 0.44 eV. The ground state Decades relitting (between 4 and T_g states at $\tilde{K}=0$) is similarly calculated to be 1.22 eV.

The additivity of pair interactions is checked, in the nearest neighbour approximation by comparing the splitting yielded by equation (9) when n is extended to

site *i* of unit cell n(i = 1, 2, 3, 4, n = 1, 2...N) by ϕ_{ni}^{S} and ϕ_{ni}^{o} for the lowest excited singlet and the ground distribution state associated as a state of the project of the ground state of $\tilde{K} = 0$ relative to the crustal ground state.

obtained agree with each other within 2%-4% in the density range between 22.47 cm³/mole and 17.5 cm³/mole.

the band relative to the free inforceme transition is

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performing a cluster calculation on one molecule surrounded by 5 orders of neighbours and analyzing the resultant one-electron energy levels to obtain the shift of the band. The result of the first calculation is $-0.10 \,\mathrm{eV}$ ringues order perturbation terms corresponding to unfer ent polarizations of the crystal by the ground and excited state are difficult to calculate and could be important in determining the Davydov shift. The experimental shift of the center of the absorption band in D-[29] is approxi-

(b) A different approach to evaluate the energies of the dipole allowed exciton states rests upon expanding the interaction potential in multipole series and retaining only mental value by a factor of 2-3, due to the neglect of other than dipole interactions and relaxation effects.*

Mixing of the T_{μ} exciton component with other T_{μ} states originating from the free molecule dipole allowed second order crystal neid effects, out will probably affect the splitting only to a small extent due to the large value of the oscillator strength to the $B^{1}\Sigma_{1\mu}$ state.

When the calculation of the splitting in the semiempirical LCAO approach is performed for various crystal

cell dimension a as $a^{-8.1}$ (Fig. 3) over the range $5.2 \le a$ 4.9 Å, which is a much stronger dependence than that anticipated by pure dipole interactions. This short range rapidly with distance. Similarly, the Davydov splitting

a dependence of $a^{-12.7}$ which is also much shorter range

and a are integers. If we denote the orientation of each sublattice by unit vectors \hat{e}_i , the angles are defined by:

potentials, respectively.

The number of pairs of states joining the valence and conduction levels respectively in the energy between $h\omega$

and M' is the molecular electronic transition dipole related to the absorption oscillator strength f by

$$|M^{s}|^{2} = \frac{3he^{2}f}{8\pi^{2}m_{e}c\bar{\nu}}$$
 (13)

where m, is the electron mass and \bar{v} is the frequency at the center of the band. For an f.c.c. lattice, the sum in ann ha angilu aughustad bu tha Niibaan and de

frequency and f as the gas phase total oscillator strength

detween A_n and I_n a value of 0.13 ev considerably lower than the value obtained by the LCAO cluster calculation, employing the full interaction. Splitting calculated according to dipole transition moments were shown in other cases to underestimate the experi

description is possible. Figure 4 describes this joint density of states, as obtained by sampling the clusters orbital energies. The edge of the absorption is now of T_u character and appears at 10.5-10.6 eV as compared with the experimental value of Baldini[29] for D₂ crystal, of $10.8 \,\mathrm{eV}$. The region above $\approx 11.3 \,\mathrm{eV}$, is of A_u character and the transition to it is forbidden. The qualitative overall shape of the spectrum is similar to the observed absorption, though quantitatively the calculated spectrum diabete nameous makable due to the medicat of the

the spectrum

isolated rig molecule and the sond, was estimated from the electronic spectrum of large radius Wannier impurity states in X_c/H_2 system[42] and in pure H_2 [43]. The impurity ionization potential in solid inert medium (c) is related to the cas phase impurity ionization

one postulated by Hexter[38]), yields in the dipole approximation

$$IP_{im}(s) = IP_{im}(g) + P_{\cdot} + V_{o} \tag{14}$$

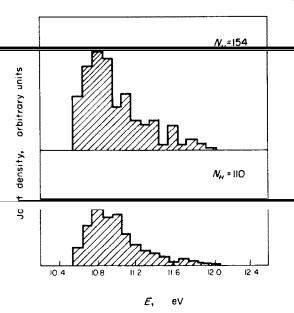


Fig. 4. Transition density of states (number of states connecting valence and conduction bands, respectively within energy range from E to $E + \Delta E$) as a function of energy, as calculated by IEXH for the 110H and 154H clusters.

energy of the medium and V_o is the energy of the quasi free electron state corresponding to the bottom of the conduction state relative to the vacuum level. Similarly, the pure solid ionization potential IP(s), is related to the ionization potential of its free constituents IP(g), by [42]:

$$IP(s) = IP(g) + P_{\perp} + V_{o} + E_{c}$$
 (15)

where E_v corresponds to the energy difference between

 X_c/H_2 system [42] together with the knowledge of the experimental value of $IP_{im}(g)$ for X_c , suggests that $-(P_+ + V_0) \sim 1-2$ eV in solid H_2 , which yields, through equation (15), taking IP(g) = 15.43 eV [26], on a ionization potential for the solid of $[13.5-14.5+E_v]$ eV $\approx 14.1-15.1$ eV. Evidence for a possible convergence limit of the Wannier series at 14.4 eV in pure solid $H_2[43]$

5. POINT DEFECTS IN SOLID H₂

The relatively large band gap and ionization potential of almost exclude processes such as simple bound optical transitions to conduction or ionized states, under conditions of irradiation with laser photons of energy in the range of 1-2 eV, as desired in experiments of laser heating of solid H₂[15, 48]. Multiphoton mechanisms[49] or generation of antistokes radiation inside the target [50] are not sufficient to enhance these absorption processes sufficiently. Another possible way of lowering the effective energy gap for such transitions, is introduction of impurities inside the solid target, thereby creating anowed electronic states in the otherwise forological gap. The truncated crystal method described in Section 2 was demonstrated to be suitable for calculation of such states in covalent crystals [2-6] because it provides a simple means of correlating the one-electron energy states of

means of correlating the one-electron energy states of localized impurities with respect to the band edges. Employment of charge self-consistent methods to calculate the one-electron energy states of a cluster containing an impurity with different electronegativity than that of the host atoms, and the allowance made for small lattice distortions and relaxations around the center, provide useful mechanisms for introducing charge and energy redistribution effects that are important in problems of deep impurity states [4, 5].

We chose to discuss here some model calculations for two impurities that may enter unpurified solid hydrogen: an isolated hydrogen atom and a nitrogen molecule. The procedure of calculation goes in the following steps: (a) We choose a large enough hydrogen molecular cluster so that the examined (Section 3) electronic properties

the origin +3 shells) exhibits a band gap, ionization potential, average charge per atom and overlap population between two bonded atoms, very close to that of the convergence limit defined as that of the largest cluster considered (Fig. 1).

(b) The central H_2 molecule at the origin is then replaced by the chosen impurity and the calculation of the

Simple theoretical calculations of $P_{+}[42]$ based on the

the cluster size from 3 to 4 and 5 shells of H₂ molecules

-0.8 eV, while a simple pseudopotential calculation [40] yields $V_o = +2.2$ eV. This disagrees both with the value of $V_o \le 0.5$ eV measured by Halpern and Gomer [47] for liquid H₂, and with the spectroscopic value of $V_o = (1.2, 0.2)$ eV mainly due to the support of the repulsive pseudopotential that was taken to depend semi-empirically on the scattering length.

(c) Once the one-electron energy levels associated with the impurity and the band edges have stabilized for a given molar volume of the cluster, we allow symmetric small ($\Delta = 0.1-0.2 \text{ Å}$) relaxations of the lattice around the unagonals of the ray unit cen, in order to examine the effect of model distortions on the defect states.

1. Hydrogen atom impurity

Table 1 summarizes the main results obtained for the H atom defect.

The energy of the impurity states is shown to become stable relative to the band edges, resulting in a net destabilization of the atomic 1s state of hydrogen relative to the free atom. The pre-electron energy state correct to the free atom.

vicinity of the atom, exerting only small perturbation on

2. Nitrogen molecule impurity

An isolated N₂ molecule is described in the IEXH frame (free atom orbital energies taken from Hartree-Fock calculation on the 'S ground state[51] and charge dependent energies form the work of Rein et al. [22]) to have an equilibrium internuclear distance of 1·15 Å

tion energy of 9.9 eV (experimental value 9.756 eV [26])

accumulates a net electron density on it of the order of $-0.02 \, e$. Inward relaxations of the lattice result in a relative destabilization effect on the defect state, while outward relaxation tend to stabilize it. It should, however, be kept in mind that the cluster model suggested does not represent adequately the real restoring forces of the covalent molecular crystal due to the lack of second order polarization forces in this closed shell LCAO picture.

molecule is placed at the origin of the Pa3 molecular hydrogen cluster and calculation steps (a)-(c) performed. The results are shown in Table 2.

The π_R orbital remains unsplit in the crystal and appears in the band gap. The lowest $2\sigma_R \to \pi_R$ molecular transition is blue shifted relative to the transition in the isolated molecule by 0·18 eV at normal density. Both $2\sigma_R$ and the π_R levels are stabilized in the crystal relative to

(Fig. 5) the impurity level approaches the edge of the conduction band being for instance already 8.7 eV from it at a = 5.0 A. The net charge accumulated on the detect

Again the guest molecule has only a small perturbative effect on the charge distribution around it, at normal density, and the hitrogen molecular bond population

Table 1. Energy states of conduction and valence band edges and impurity state for relaxed ($\Delta = 0.2 \text{ Å}$) and unrelaxed lattice for the H-impurity clusters

	Conduction		Impurity state (eV)		
S		Valence	No	Inward	Outward
1 + 36	4.431	13.098	13:419	13.398	13.378
I + 42	4.455	15.065	13-418	13.399	13.580
1 - 54	4.456	15.065	13.417	13.399	13.580
1 + 76	4.456	15.063	13-417	13.399	13.580

Table 2. Energy states of conduction and valence band edges and impurity state for relaxed ($\Delta = 0.2 \text{ Å}$) and unrelaxed lattice for the N₂ impurity clusters

Cluster	Conduction edge (eV)	Valence edge (eV)	$\pi_{\rm g}$ Impurity state (eV)		
			No relaxation	Inward relaxation	Outward relaxation
I + 36	4.447	15.094	11.099	11.030	12.050
I + 42	4.455	15.066	11.098	11.032	12.052
I + 54	4.456	15.065	11.098	11.033	12.054
1 + 76	4.456	15.065	11.098	11.034	12:054

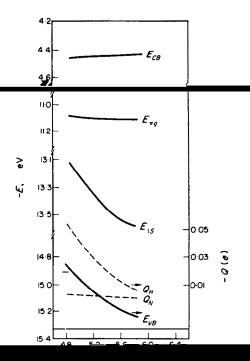


Fig. 5. Variation of some electronic properties for the defect crystal problem. E_{CB} and E_{VB} : energies of the edge of conduction and valence bands respectively (with N_2 impurity). $E_{\pi\pi}$: one electron defect state of $N_2\pi_e$ level, E_{1*} : one electron defect state of H 1S level Q_H , Q_N : net atomic charges of H and N atoms in the cluster.

ress electronegative hydrogen molecules surrounding it.
Relaxation of the lattice around the impurity molecule results in relatively small shifts of the impurity level.

6. SUMMARY

We have used the terrested emotel emores with

several densities, as a function of cluster size for "spherical" clusters. Information regarding density effects on charge distribution and one electron energy

crystal states as well as localized defect states in a unified model when the convergence limit is reached and in the simple way of introducing self-consistent charge redistribution and relaxation effects. The main shortcomings of lack of configuration interaction in the calculation, which are both presently excluded due to limitation in computer storage.

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interactions, neglecting three and multicenter integrals and

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- C. 7, 2467 (1974)] using a spherical approximation to the Columb molecular potential including three forms of exchange (Slater^(a), Lundqvist-Lundqvist^(b) and Khon-Sham^(c)) in a non-self-consistent treatment. The following table summarizes the results:

Property	Monnier et al.	Gomez et al.	Present work	Expt.
IP (solid) eV	19-1 ^(a) 15-5 ^(b)	15-82	15-1	14·5 ^(f)
Band width eV	14·2 ^(c) 0·369 ^(a) 0·825 ^(b)	1.1	1.22	_
Eg eV	0.945 ^(c) 12.029 ^(a) 9.276 ^(b)	_	10.7	$\sim\!10\!\cdot\!8^{\text{(d)}}$
JP (molecule) eV	8·789 ^(c) 15·0	16-135	15-38	15·43 ^(e)
(molecule) eV	3.488	3-488	4-66	4·474'°

⁽a) Slater exchange [J. C. Slater, Phys. Rev. 81, 385 (1951)].

- (c) Kohn and Sham exchange [W. Khon and L. J. Sham, Phys. Rev. 140A, 1133 (1965)].
- (d) Ref. 29.
- (e) Ref. 26.
- (f) Ref. 43.

In this table, IP (solid) denotes the negative of the highest occupied valence band state (Γ_4 in the notation of Gomez et al. and K_1 in the notation of Monnier et al.) and E_a denotes the transition between the Γ_4 and Γ_4' states ($K_1 \rightarrow K_4$ in the notation of Monnier and $\Gamma_4 \rightarrow \Gamma_4$ in the notation of the present paper). The

Parravicini and M. Vittori, unpublished), using a nonlocal exchange potential in the zero-overlap approximation and a Coulamb potential from the Slater 1s charge density, the lowest conduction state was calculated to be of Γ_1 symmetry and this state was separated by a gap of 13-8 eV from the top of the valence band. The

present work and the works of Gomez et al. and Monnier et al. In a

work $(L_n = 10.7 \text{ eV})$ and the observed edge of the absorption edge of Baldini, 10.8 eV [29].

⁽b) Lundquiet Lundquiet exchange IP. I Lundquiet and S. Lundquiet Computational Solid