

# Ordering tendencies in octahedral MgO-ZnO alloys

Mahdi Sanati,<sup>1</sup> Gus L. W. Hart,<sup>2</sup> and Alex Zunger<sup>1</sup>

<sup>1</sup>*National Renewable Energy Laboratory, Golden, Colorado 80401, USA*

<sup>2</sup>*Department of Physics & Astronomy, Northern Arizona University, Flagstaff, Arizona 86011-6010, USA*

(Received 18 August 2003; published 24 October 2003)

Isostructural II-VI alloys whose components are either rocksalt stable (e.g., CaO-MgO) or zincblende stable (e.g., ZnS-ZnSe) are known to be thermodynamically unstable at low temperatures, showing a miscibility gap and no bulk ordering. In contrast, we show that *heterostructural* MgO-ZnO is stable, under certain conditions, in the sixfold-coordinated structure for Zn concentrations below 67%, giving rise to spontaneously ordered alloys. Using first-principles calculations, we explain the origin of this stability, the structures of their low-temperature ordered phases, short-range-order patterns, and their optical band-gap properties.

DOI: 10.1103/PhysRevB.68.155210

PACS number(s): 71.55.Gs, 71.20.Nr

## I. INTRODUCTION

Binary II-VI compounds appear<sup>1</sup> largely as fourfold-coordinated (CN4) zincblende/wurtzite structures (ZnO, ZnS, ZnSe, ZnTe, CdS, CdSe, and CdTe) or as sixfold-coordinated (CN6) rocksalt structures (MgO, CaO, and CdO). Isovalent and isostructural alloys of II-VI constituents are generally thermodynamically unstable, in that their mixing enthalpy, in either the CN6 rocksalt (*B1*) structure or in the CN4 (*B3*) or wurtzite (*B4*) structures,

$$\Delta H_{\alpha}(A_xB_{1-x}C) = E_{\alpha}(A_xB_{1-x}C) - [xE_{\alpha}(AC) + (1-x)E_{\alpha}(BC)], \quad (1)$$

is *positive*.<sup>2-4</sup> Here,  $\alpha$  denotes fourfold or sixfold coordinated crystal structure, and  $E_{\alpha}(AC)$

functional for  $\sim 3 \times 10^6$  possible configurations, we identify  $\text{Mg}_3\text{ZnO}_4$  ( $D0_{22}$ ) and  $\text{Mg}_4\text{Zn}_4\text{O}_8$  as ordered  $B1$ -like ground-state structures.

(5)

are the most stable. To answer this we have parametrized 32 *B1* total-energy calculations of  $\text{Mg}_m\text{Zn}_n\text{O}_{m+n}$  structures (shown as open squares in Fig. 2) into a cluster expansion. Within the cluster-expansion method<sup>7</sup> one selects an under-

differences within 0.3 meV/atom. Although several “breaking points” exist, the energetically “deepest” structures occur at  $x=0.25$  and  $x=0.5$ . For  $x=0.25$ , the ground state is a  $DO_{22}$ -type structure with lattice constants  $a=4.174$  Å and  $c=4.179$  Å. For  $x=0.50$ , the ground state is an orthorhombic structure with lattice constants  $a=4.189$  Å,  $b=4.187$  Å, and  $c=8.900$  Å. The atomic positions and lattice vectors of predicted ground states are shown in Table III. The common structural motif for these ground-state structures is that they are (201) superstructures. It is known that (201) superstructures have low Madelung energies<sup>7</sup> and our calculations show that the constituent strain energy along the (201) direction is softer with respect to the other principal directions.

### C. Thermodynamic modeling

Figure 2 shows the energy of the random  $B1$  solid solutions (solid line), obtained by performing high-temperature (40 000 K) Monte Carlo simulations with Hamiltonian,  $E_{CE}(\cdot)$ . The open symbols denote the energies of ordered structures, used as input to the cluster expansion, whereas the energies of the ground-state structures are denoted by solid squares. We see that the energy difference between the stable ordered ground-state structures and the random alloy of the same composition (e.g.,  $x=0.5$ ) is rather small ( $-6.5$  meV/

cation), so the order-disorder transition temperature will be well below conventional growth temperatures (e.g.,

sab

at high temperatures. The random alloy has an LDA band gap of 2.49 eV at  $x=0.5$  (using a special quasirandom structure<sup>17</sup>), and hence a bowing coefficient  $b_{\text{bowing}} = 3.10$  eV, where  $E_g(x) = (1-x)E_{\text{MgO}} + xE_{\text{ZnO}} - x(1-x)b_{\text{bowing}}$ . This value of the bowing coefficient is in good agreement with the value of  $3.6 \pm 0.6$  eV measured recently by Schmidt *et al.*<sup>10</sup> The ordered structure at  $x=0.5$  has a lower band gap than the random alloy by 0.39 eV. There is a CN6 to CN4 transition for  $x_{\text{Zn}} > 0.67\%$ , whereas the coher-

ent alloy is  $B1$  stable below this composition. If MgO and ZnO can (incoherently) adopt their own crystal structures ( $B1$  and  $B4$ , respectively), the alloy is predicted to phase separate.

#### ACKNOWLEDGMENT

This work was supported by the U.S. D8 0 ACKN