

## Band structure and stability of zinc-blende-based semiconductor polytypes

Su-Huai Wei, S. B. Zhang, and Alex Zunger

National Renewable Energy Laboratory, Golden, Colorado 80401

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Using a first-principles generalized one-dimensional Ising model we have studied the band structure and stability of two types of zinc-blende-based polytype series: type-a  $\text{GaInP}_2$  and type-b  $\text{CuInSe}_2$ . The interaction parameters for the formation energy are found to be short range, while the convergence is slower for the band-gap and conduction-band energies of the type-a  $\text{GaInP}_2$  polytypes. We predict that the CuAu-like phase can coexist in nominally chalcopyrite  $\text{CuInSe}_2$  and  $\text{CuInS}_2$ , while such coexistence is less likely in  $\text{CuGaSe}_2$ . We also predict that type-II band alignment can exist between different ordered type-a  $\text{GaInP}_2$  polytypes, despite that the band alignment between ordered and disordered  $\text{GaInP}_2$  are predicted to be type I. [S0163-1829(99)51804-3]

$A_{1/2}B_xC$  semiconductor alloys grown epitaxially on (001) substrate often exhibit atomic ordering,<sup>1</sup> manifested, e.g., by the CuPt-like structure<sup>2</sup> [Fig. 1(a)] in  $A^{\text{III}}B^{\text{III}}C^{\text{V}}$  compounds ( $\text{GaInP}_2$ ,  $\text{AlInAs}_2$ , and  $\text{GaInAs}_2$ ), and by the chalcopyrite structure<sup>3</sup> [Fig. 1(c)] in the  $A^{\text{I}}B^{\text{III}}C^{\text{VI}}$  compounds ( $\text{CuInSe}_2$ ,  $\text{CuInS}_2$ , and  $\text{CuGaSe}_2$ ). Unlike classic cases of long-range order in metallurgical systems, semiconductors often show surprisingly a coexistence of domains of a few types of ordered structures in the same sample. For example, epitaxial samples of nominally chalcopyrite  $\text{CuInS}_2$  exhibit electron diffraction evidence<sup>4</sup> of the CuAu-like [Fig. 1(d)] ordered phase. Also, nominally CuPt-like  $\text{GaInP}_2$  samples have been suggested to contain a Y2-like phase<sup>5</sup> [Fig. 1(b)], antiphase boundaries (APB) on the (001) planes,<sup>6</sup> and “orientational superlattices”<sup>7</sup> with periodically alternating (111) and (11 $\bar{1}$ ) ordered subvariants.<sup>8,9</sup> Such samples with mixed ordering domains often exhibit interesting optical effects such as localized excitons,<sup>10</sup> spatially indirect interband transitions in magnetic field,<sup>11</sup> and excitation intensity dependent emission energies.<sup>12</sup> However, attempts to identify the microstructure responsible for these highly unusual effects in an ordered compound have failed. For example, the suggested<sup>11-13</sup> coexistence of CuPt-ordered domains with random-alloy domains cannot explain the spatially indirect transitions since the offset in this system is type I.<sup>14,15</sup>

In this paper, we provide an easy and systematic way to study theoretically the electronic and structural properties of the mixed-phases ordered semiconductor compounds discussed above. We show that these ordered structures can be formed by different stacking of basic (001) atomic planes, i.e., they are polytypes.<sup>16</sup> The physical properties, such as the formation energies, band gaps, and band offsets of any member of a polytype series can be predicted systematically using a generalized one-dimensional Ising model,<sup>17</sup> where the Ising interaction parameters are obtained from accurate, first-principles electronic structure calculation on a few (small unit cell) polytypes. We find that  $\text{CuInSe}_2$  polytypes have very similar formation energies (thus, explaining phase coexistence in this system) and that certain  $\text{GaInP}_2$  polytype pairs manifest a “type-II” band alignment, thus holding the potential for explaining the puzzle of exciton localization

and spatially indirect interband transitions in chemically homogeneous and highly ordered compounds.<sup>10-13</sup>

We discuss here two classes of polytypes for the 50%-50% compounds  $ABC_2$ . Unlike the well studied case of hexagonal/cubic SiC and ZnS polytypes,<sup>16</sup> here we discuss the case of pure fcc polytypes. Figure 2 shows the basic (001) atomic plane from which the two polytypes are constructed. For both planes, a uniform shift of the plane by  $\tau \approx 5(1/2, 1/2, 0)a$  is equivalent to the permutation of  $A$  to  $B$ . In the type-a plane [Fig. 2(a)], the  $A$  and  $B$  atoms form alternating lines along the [110] direction. The polytypes that can be constructed by stacking the type-a plane on an fcc lattice include the CuPt [Fig. 1(a)] and the Y2 [Fig. 1(b)] structures. All the type-a polytypes  $ABC_2$  contain equal numbers of

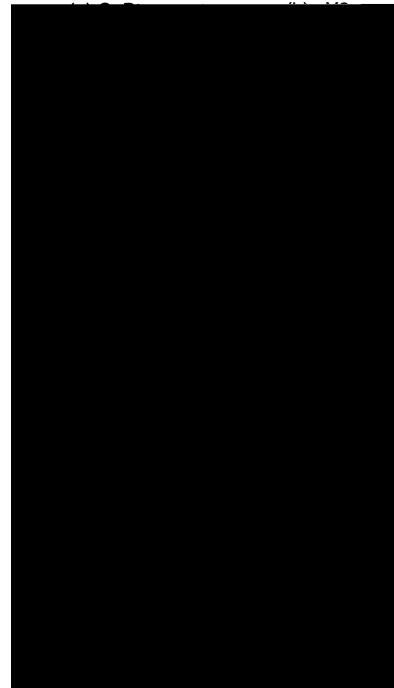


FIG. 1. Crystal structures of (a) CuPt, (b) Y2, (c) chalcopyrite, and (d) CuAu pseudobinary semiconductor compounds. CuPt and Y2 belong to type-a polytypes while chalcopyrite and CuAu belong to type-b polytypes.

$A_3B$  and  $AB_3$  tetrahedral clusters around the common  $C$  atom [Figs. 1(a) and 1(b)]. In the type-b plane

method,<sup>20</sup> the total-energy, band-gap energy and the energy lineups of the valence-band maximum (VBM) and conduction-band minimum (CBM) of four GaInP<sub>2</sub> polytypes:  $\langle\infty\rangle$ ,  $\langle 2\rangle$ ,  $\langle 3\rangle$ , and  $\langle 4\rangle$  belonging to the type-a series. From these four calculated LDA values we then determine four interactions ( $J_0$ ,  $J_2$ ,  $J_4$ , and  $J_6$ ) for each physical property. Using this calculated  $\{J_{k\leq 6}\}$  we then predict from Eq. (1) the properties of other polytypes, not used in the fit. Table II shows the directly calculated LDA results for the GaInP<sub>2</sub> polytypes, and in parentheses, the values obtained from the Ising expansion, using the fitted  $\{J_{k\leq 6}\}$ . Figure 4 plots the band-gap energy and the VBM and CBM energies as a function of the layer thickness  $n$  of the APB superlattice  $\langle n\rangle$ . Similar calculations were performed for type-b polytypes CuInSe<sub>2</sub> (Table III). We note the following observations.

(i) *Formation energies.* The Ising expansion converges rapidly for the formation energies. Within the accuracy of the underlying LAPW calculation, one needs to retain only  $J_2$  and  $J_4$  for the GaInP<sub>2</sub> polytypes. For the CuInSe<sub>2</sub> polytypes, only  $J_2$

little effect on their electrical and optical properties. In contrast,  $E_g(\text{CH}) \approx E_g(\text{CuAu}) \approx 232$  meV for  $\text{CuGaSe}_2$ . Thus, the effect is larger for  $\text{CuGaSe}_2$ .