

Predicting Criticality and Dynamic Range in Complex Networks: Effects of Topology

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Temporal chaos is a well-known phenomenon in complex networks. However, the criticality of a network is a less well-understood concept. We study the criticality of a network by analyzing the dynamics of a system of coupled oscillators. We show that the criticality of a network is determined by the topology of the network. We also show that the dynamic range of a network is determined by the topology of the network. Our results show that the criticality and dynamic range of a network are both determined by the topology of the network.

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Networks are ubiquitous in nature and have been studied extensively in recent years [1,2]. A network is a collection of nodes (or vertices) connected by edges (or links). The topology of a network refers to the arrangement of its nodes and edges. The criticality of a network is a measure of its ability to sustain a phase transition. The dynamic range of a network is a measure of its ability to sustain a wide range of behaviors. In this paper, we study the criticality and dynamic range of a network by analyzing the dynamics of a system of coupled oscillators. We show that the criticality of a network is determined by the topology of the network. We also show that the dynamic range of a network is determined by the topology of the network. Our results show that the criticality and dynamic range of a network are both determined by the topology of the network.

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