### APPM 1345

APPM 1345		
AIT W 1343	Name	
Exam 3		
Spring 2023	Instructor Richard McNamara	Section 150
Spring Zuzs		

This exam is worth 100 points and has 4 problems.

Make sure all of your work is written in the blank spaces provided. If your solutions do not fit, there is additional space at the end of the test. Be sure to make a note indicating the page number where the work is continued or it will not be graded.

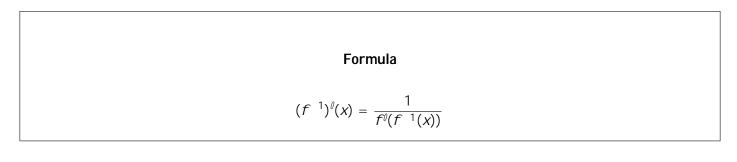
**Show all work and simplify your answers.** Name any theorem that you use. Answers with no justification will receive no points unless the problem explicitly states otherwise.

Notes, papers, calculators, cell phones, and other electronic devices are not permitted.

#### End-of-Exam Checklist

1. If you finish the exam before 7:45 PM:

- · Go to the designated area to scan and upload your exam to Gradescope.
- Verify that your exam has been correctly uploaded and all problems have been labeled.
- Leave the physical copy of the exam with your proctors.
- 2. If you finish the exam after 7:45 PM:
  - Please wait in your seat until 8:00 PM.
  - When instructed to do so, scan and upload your exam to Gradescope at your seat.
  - Verify that your exam has been correctly uploaded and all problems have been labeled.
  - Leave the physical copy of the exam with your proctors.



- 1. (23 pts) Parts (a) and (b) are unrelated.
  - (a) Find the inverse function of  $g(x) = 6x^5$  1.

# Solution:

$$y = g(x) = 6x^5 \quad 1$$
$$6x^5 = y + 1$$
$$x^5 = y + 1$$

- 2. (27 pts) Parts (a), (b) and (c) are unrelated.
  - (a) Suppose 1=3 of a radioactive substance remains after decaying exponentially for 10 years. Find the half-life of the substance, including the correct unit of measurement. Fully support your answer.

#### Solution:

Since the substance is undergoing exponential decay, the amount of the substance at time t years can be represented by  $y(t) = y_0 e^{kt}$ , where  $y_0 = y(0)$  is the amount of the substance at time t = 0 and k is the relative rate of change. Therefore, for t = 10, we have the following:

$$y(10) = y_0 e^{10k} = \frac{y_0}{3}$$
 )  $10k = \ln \frac{1}{3}$  )  $k =$ 

3. (24 pts) Evaluate the following derivatives using properties of logarithms and/or logarithmic differentiation. Do **not** fully simplify your answers, although they must be expressed as functions of *x*.

(a) 
$$\frac{d}{dx} \ln \frac{(x-2)^{3=2}(\cos x+2)}{\sqrt{x^2+4}}$$
,  $x > 2$ 

Solution:

$$\frac{d}{dx} \ln \frac{(x-2)^{3=2}(\cos x+2)}{\sqrt[3]{x^2+4}} = \frac{d}{dx} \ln \binom{h}{n}$$

4. (26 pts) Evaluate the following integrals. Fully simplify your answers.

(a) 
$$\int_{4}^{2} \varphi \frac{dx}{\overline{x}(1-2)} \varphi \overline{\overline{x}(1-2)}$$

Solution:

Let u = 1  $2^{p}\overline{x} = 1$   $2x^{1=2}$ , which implies that  $du = x^{1=2} dx = \oint_{\overline{x}}^{dx}$ . x = 4 ) u = 1  $2^{p}\overline{4} = 3$  x = 9 ) u = 1  $2^{p}\overline{9} = 5$  $Z_{9} = \oint_{\overline{x}(1-2^{p}\overline{x})}^{Z} = Z_{3}^{5} \frac{du}{u} = Z_{5}^{3} \frac{du}{u} = \ln juj$   $\frac{3}{5} = \ln$ 

Your Initials \_\_\_\_\_

# ADDITIONAL BLANK SPACE If you write a solution here, please clearly indicate the problem number.